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Band anticrossing in dilute nitrides

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Abstract

Alloying III–V compounds with small amounts of nitrogen leads to a dramatic reduction of the fundamental band-gap energy in the resulting dilute nitride alloys. The effect originates from an anticrossing interaction between the extended conduction-band states and localized N states. The interaction splits the conduction band into two non-parabolic subbands. The downward shift of the lower conduction subband edge is responsible for the N-induced reduction of the fundamental band-gap energy. The changes in the conduction band structure result in a significant increase in electron effective mass and a decrease in the electron mobility, and lead to a large enhancement of the maximum doping level in GaInNAs doped with group VI donors. In addition, a striking asymmetry in the electrical activation of group IV and group VI donors can be attributed to mutual passivation process through formation of the nearest neighbour group-IV donor nitrogen pairs.

1. Introduction

Dilute nitrides have recently attracted considerable attention. It has been found that the substitution of the group V anions in conventional III–V compounds with small amounts of nitrogen leads to dramatic changes of the electronic properties. These include a reduction of the fundamental band-gap energy [1, 2], a significant increase in electron effective mass and a decrease in electron mobility [3–5]. Furthermore, a new optical transition (E_+) above the fundamental band-gap energy has been observed [6, 7]. As one quantitative example, the incorporation of only 1% of nitrogen into GaAs induces a strikingly large reduction of 0.18 eV in the fundamental band-gap energy [8]. This reduction is much larger than the changes observed when alloying different III–V compound semiconductors at the per cent level.

It is now generally accepted that the unexpectedly strong effect of N on the band gap is related to the fact that replacement of atoms such as As with the much smaller and more electronegative N atom leads to a large, local perturbation of the crystal lattice potential. Extensive experimental and theoretical studies over the past decade have led to several proposals aimed at understanding the origin of the large band gap reduction [9–26]. In this paper, we show that the effect of nitrogen on the electronic band structure of dilute nitrides can be consistently described in terms of an anticrossing interaction between localized nitrogen states and the extended conduction-band states of the semiconductor matrix [6, 27]. The interaction leads to a significant modification of the band structure of the dilute III–N–V alloys. All the dramatic changes of the electrical and optical properties that have been observed experimentally can be fully explained by this interaction.

2. Band anticrossing model

It is well known that an isolated N atom introduces a localized state with energy level E_N in conventional III–V materials. In most cases, this level is located very close to the conduction band edge. It lies at about 0.25 eV above the conduction band edge in GaAs and less than 0.1 eV below the conduction band edge in GaP. The existence of such states has been predicted by theoretical calculations within the tight binding approximation framework [28], and confirmed by experimental measurements under hydrostatic pressure [29, 30]. As expected for a localized state, a much weaker pressure dependence of the N energy level was observed in GaAs compared to the conduction-band edge. The level was also found to move into the band gap when GaAs is alloyed with AlAs [31]. The highly localized nature of the N states suggests that there is only weak hybridization between the orbits of N atoms and the extended states, $E_M(k)$, of the semiconductor matrix. The electronic band structure of the host crystal is not significantly affected by these low nitrogen concentrations. However, alloying a few atomic percent of nitrogen with III–V compounds drastically modifies the electronic band structure.

In considering the problem of the profound changes in the band structure of the resulting dilute III–N–V nitrides, we assume that N atoms are randomly distributed over the group V sites and are only weakly coupled to the extended states of the host semiconductor matrix. The eigenvalue problem can then be written as

$$\begin{vmatrix} E_{\rm M}(k) - E(k) & V_{\rm MN} \\ V_{\rm MN} & E_{\rm N} - E(k) \end{vmatrix} = 0,$$
(1)

where $E_{\rm M}(k)$ and $E_{\rm N}$ are the energies of the unperturbed conduction band and of the localized states relative to the top of the valence band, respectively. $V_{\rm MN} = \langle k | V | N \rangle$ is the matrix element describing the coupling between N-states and the extended conduction-band states, $V = \Sigma_{\rm s} U(\mathbf{r} - \mathbf{R}_{\rm s})$, and $U(\mathbf{r} - \mathbf{R}_{\rm s})$ is the potential introduced by an N atom on a $\mathbf{R}_{\rm s}$ site. The solution of equation (1) takes the form

$$E_{\pm}(k) = \frac{1}{2} \left\{ (E_{\rm M}(k) + E_{\rm N}) \pm \sqrt{(E_{\rm M}(k) - E_{\rm N})^2 + 4V_{\rm MN}^2} \right\}.$$
 (2)

The squared matrix element coupling k and N states, is given by [27]

$$|V_{\rm MN}|^{2} = \langle k|V|N\rangle\langle N|V|k\rangle = \Sigma_{\rm s}\Sigma_{s'}\int\int V^{-2}\,\mathrm{d}\mathbf{r}\,\mathrm{d}\mathbf{r'}\,\mathrm{e}^{\mathrm{i}kr}\,U^{*}(\mathbf{r}-\mathbf{R}_{\rm s})\Psi_{\rm N}^{*}(\mathbf{r}-\mathbf{R}_{\rm s})$$
$$\times U(\mathbf{r'}-\mathbf{R}_{s'})\Psi_{\rm N}(\mathbf{r'}-\mathbf{R}_{s'})\,\mathrm{e}^{-\mathrm{i}kr'}.$$
(3)

 $\Psi_{\rm N}(\mathbf{r})$ is the wavefunction of the N state localized on the substitutional site. Equation (3) is valid for low N concentrations when there is no appreciable overlap between functions $S(\mathbf{r} - \mathbf{R}_{\rm s}) = U(\mathbf{r} - \mathbf{R}_{\rm s})\Psi_{\rm N}(\mathbf{r} - \mathbf{R}_{\rm s})$ located on different sites. Using the Fourier transform of the function $S(\mathbf{r})$, $V_{\rm NM}$ can be written as

$$|V_{\rm MN}|^2 = |S(k)|^2 \{ \Sigma_{\rm s} \Sigma_{s'} \exp[i\mathbf{k}(\mathbf{R}_{\rm s} - \mathbf{R}_{s'})] \}.$$
⁽⁴⁾



Figure 1. Illustration of the effects of band anticrossing on the conduction-band structure in the vicinity of the Γ -point minimum. (a) The highly electronegative isoelectronic N induced localized state resonant with the conduction band; (b) the localized state located below the conduction band. The solid curves are the restructured E_{-} and E_{+} subbands resulting from the band anticrossing interaction between the localized states (dash–dotted line) and the extended states of the conduction band (broken line).

The double sum in equation (4) has to be averaged over all possible N atom configurations in the host crystal lattice. For a random distribution it equals the total number of substitutional N atoms which is proportional to the molar fraction of N in the alloys. Therefore the matrix element can be written as $V_{\rm MN} = C_{\rm MN} x^{1/2}$, where $C_{\rm MN}$ is a constant describing the coupling between localized states and the extended states of the semiconductor matrix and x is the alloy composition. The interaction of the conduction-band edge with the dispersionless N level results in a splitting of the conduction band into two highly non-parabolic subbands, $E_{-}(k)$ and $E_{+}(k)$. The energy positions of the subband edges E_{-} and E_{+} given by equation (2) depend on alloy concentration x and the coupling parameter $C_{\rm MN}$, as well as the location of $E_{\rm N}$ with respect to the conduction band edge $E_{\rm M}$.

Figure 1 shows schematic examples of the calculated band structure based on the BAC model. The interaction between the localized isoelectronic states and the extended conductionband states has a pronounced effect on the dispersion relation of the two conduction subbands E_- and E_+ . The effect of the interaction is most pronounced for the states located close to E_N . If the localized state is located within the conduction band of the matrix, as depicted in figure 1(a), the conduction-band states at the E_- edge retain mostly the extended E_M -like character and those at the E_+ edge have a more localized and E_N -like character. The lower conduction subband narrows drastically as the energy position of the E_N level moves down relative to the bottom of the conduction band. Narrowing of the band indicates a gradually increased contribution of the localized nature to the lowest subband, leading to a highly non-parabolic dispersion relationship that induces an enhancement of the effective mass and the density of states in the lower subband. If the localized state is located below the conduction-band edge, as illustrated in figure 1(b), the conduction-subband edges E_- and E_+ switch their character: the E_- subband states assume a highly localized nature and the E_+ subband states possess the character of the extended state. The electron effective mass as a function of energy can be calculated using the standard definition of the density of states effective mass,

$$m_{-}^{*}(\mathbf{k}_{\rm F}) = \hbar^{2} \left| \frac{k}{\mathrm{d}E_{-}(\mathbf{k})/\mathrm{d}k} \right|_{k=\mathbf{k}_{\rm F}} = m_{0}^{*} \left[1 + \frac{C_{\rm MN}^{2} x}{(E_{\rm N} - E_{-}(\mathbf{k}_{\rm F}))^{2}} \right],\tag{5}$$

where m_0^* is the effective mass of the semiconductor matrix and *E* is the energy in the lower or upper subband measured from the valence band edge. It is seen from equation (5) that the effective mass diverges for the electron energy approaching E_N . This is a result of the increasing contribution of the localized N states to the electron states in the lower and upper subbands.

Recent theoretical considerations using the tight binding approximation have provided additional refinements for the BAC model [32, 33]. It has been argued that the conventional $\mathbf{k} \cdot \mathbf{p}$ model must be modified to include two extra spin-degenerate nitrogen states so as to use ten bands to describe the electronic band structure of GaNAs/GaAs and related heterostructures. In addition, detailed studies on the nearest neighbour environment of the substitutional N atoms in GaInNAs have shown that the fundamental band-gap energy in quaternary dilute nitride alloys is fairly sensitive to the local environmental conditions, especially in the case of quantum well structures [34, 35].

3. Experimental results and discussion

3.1. Samples

A large variety of dilute III–N–V nitrides including GaNAs, GaInNAs, AlGaNAs, GaNP and InNP have been extensively studied over the past few years. The majority of the samples used in the studies discussed below were grown by either metalorganic vapour phase epitaxy (MOCVD) with dimethylhydrazine as nitrogen source, or gas-source molecular beam epitaxy (MBE) using a RF plasma nitrogen radical beam source. The nitrogen contents in those samples were determined using secondary ion mass spectrometry (SIMS) and indirectly from the change of the lattice constant measured with the (004) reflection in double-crystal x-ray diffraction.

A new method for synthesizing dilute nitrides was developed during the course of the studies. We have found that nitrogen implantation followed by rapid thermal annealing (RTA) is a practical and convenient method for the formation of diluted III–N–V alloys [36, 37]. The fundamental band-gap energy for the ion beam synthesized thin films of GaN_xAs_{1-x}, InN_xP_{1-x} and Al_yGa_{1-y}N_xAs_{1-x} after N⁺ implantation into GaAs, InP and Al_yGa_{1-y}As was found to decrease with increasing N implantation dose in a manner similar to that observed in epitaxially grown thin films. In GaN_xAs_{1-x} the highest value of x achieved using N⁺-implantation and the conventional RTA technique was 0.006; this corresponds to a N activation efficiency of ~15%. In the course of optimizing the annealing conditions in these studies, it was found that, in GaNAs formed in this way, the substitutional N_{As} is thermally unstable at temperatures higher than 850 °C and will precipitate to form N-related voids [38].

Most recently, we have shown that pulsed laser melting (PLM) of N-implanted III–Vs dramatically improves the incorporation of N in the group-V element site [39, 40]. In PLM, the near surface absorption of a single intense laser pulse instantaneously melts the implant-damaged or amorphized layer. This is followed immediately by rapid epitaxial regrowth from the liquid. Epitaxy is seeded at the solid–liquid interface by the crystalline bulk in a manner very similar to liquid phase epitaxy (LPE) but with the whole process occurring on a much shorter timescale, typically between 10^{-8} and 10^{-6} s [41, 42]. Figure 2 shows a series of



Figure 2. PR spectra measured from a series of samples implanted with increasing amounts of N (x_{imp}) and processed by PLM at an energy fluence of 0.34 J cm⁻² and subsequent RTA at 950 °C for 10 s.

photoreflectance (PR) spectra from GaAs implanted with increasing amounts of N processed by PLM with an energy fluence of $0.34 \text{ J} \text{ cm}^{-2}$ and subsequently by RTA at 950 °C for 10 s. Such PLM-RTA post-implantation treatments represent the 'optimum' process conditions found to date and the samples so formed have clear, sharp optical transitions. The amount of N incorporated in the As sublattice ('active' N) for the GaN_xAs_{1-x} layers formed by this method can be estimated using the BAC model and is ~40–60% of the implanted value. This is over five times higher than that observed in samples processed by RTA only [37]. Such a drastic improvement can be attributed to the extremely short melt duration (~2 × 10⁻⁷ s) and re-growth process that promotes N substitution in the As site and inhibits the formation of nitrogen related voids [38]. In addition to the enhanced N incorporation, the dilute nitride layers synthesized by N⁺-implantation followed by PLM-RTA were also found to be thermally stable up to annealing temperature >950 °C. This improved sample synthesis technique provides a convenient and reliable method, in addition to conventional epitaxial growth techniques [2, 4, 12], for preparing a large variety of dilute nitride samples.

3.2. Direct evidence of band splitting and related anticrossing characteristics

The key result of the BAC model is that it predicts a splitting of the conduction band into two non-parabolic subbands with energy minima at E_{-} and E_{+} . The conduction band splitting has been unambiguously observed in $\text{GaN}_x \text{As}_{1-x}$ and $\text{Ga}_{1-y} \text{In}_y \text{N}_x \text{As}_{1-x}$ using photomodulation spectroscopy [6, 43]. Shown in figure 3 are PR spectra recorded with MOCVD-grown $\text{GaN}_x \text{As}_{1-x}$ samples. The PR curve of GaAs (x = 0) exhibits two sharp derivative-like



Figure 3. PR spectra of $GaN_x As_{1-x}$ samples with different N concentrations.

spectral features corresponding to the transition from the top of valence band to the bottom of the conduction band (E_0 transition), and the transition between the spin-orbit split-off band and the conduction-band minimum ($E_0 + \Delta_0$ transition). For N containing samples, in addition to the PR spectral features related to the transition across the fundamental band gap (E_- transition) and the transition from the top of the spin-orbit split-off valence band to the bottom of the conduction band ($E_- + \Delta_0$ transition), an extra feature (E_+) appears at higher energies in the PR spectra. With increasing N concentration, the E_- and $E_- + \Delta_0$ transitions shift to lower energy, as commonly observed in GaN_xAs_{1-x}, and the E_+ transition moves in the opposite direction toward higher energy, indicating that the E_- subband edge shifts downward and the E_+ subband edge moves to the other direction with respect to the top of the valence band.

The predictions of the BAC model are further verified by the measurement of the E_{-} and E_{+} transitions under applied pressure. Application of hydrostatic pressure shifts the bottom of the conduction band above the localized N level, gradually changing the character of the E_{-} -subband edge from extended E_{M} -like to localized E_{N} -like, and the character of the E_{+} -subband edge from the localized-like to extended-like. Such a transformation can be schematically visualized by figure 1. The dispersion relations of the $E_{-}(k)$ and $E_{+}(k)$ conduction subbands shown in figure 1(a) represent the case at low pressures where the bottom of the conduction band of the host matrix (E_{M}) is below the E_{N} level. Figure 1(b) represents the case at high pressures where E_{M} is shifted to above the E_{N} level. The effect of hydrostatic pressure on the optical transitions associated with the E_{-} and E_{+} subband edges in a GaN_{0.015}As_{0.985} sample and a Ga_{0.95}In_{0.05}N_{0.012}As_{0.988} sample is shown in figure 4. The anticrossing behaviour of two strongly interacting energy levels with



Figure 4. Effects of pressure on the optical transitions associated with the E_{-} and E_{+} transitions in GaN_{0.015}As_{0.985} and Ga_{0.95}In_{0.05}N_{0.012}As_{0.988}.

distinctly different pressure dependencies is unmistakably observed. The E_{-} transition has a strong dependence at low pressures and gradually saturates at high pressures, whereas the E_{+} transition has a weak dependence upon pressure at low pressures and displays a much stronger dependence at high pressures. The solid lines through the experimental data in the figure are the results of calculations using equation (2). The best fits to the data yield the energy of the nitrogen state, $E_{\rm N} = E_V + 1.65$ eV, for both samples at atmospheric pressure, and it is independent of In concentration [6, 43]. These results prove that the effects of alloying with In on the band gap can be separated from the shifts produced by the interaction with N states, allowing for an independent determination of $E_{\rm M}$ from a given In concentration in $Ga_{1-y}In_yN_xAs_{1-x}$ alloys.

To further verify that the observed E_+ transition in dilute nitrides results from the N-induced conduction-band splitting and to clarify the role of the higher conduction-band L and X minima on the E_+ transition, the effect of N on the band structure of $Al_yGa_{1-y}As$ has also been studied. It has been well established that, with increasing Al concentration, the Γ band edge shifts from below to above the L and X conduction valleys in $Al_yGa_{1-y}As$. This relative energy shift should strongly affect the strength of the interaction between those levels. Energy positions of the experimentally observed E_+ and E_- transitions for $GaN_{0.0085}As_{0.9915}$ and four $Ga_{1-y}Al_yN_xAs_{1-x}$ samples synthesized by N⁺ implantation followed by RTA treatment are shown in figure 5. The dependencies of the Γ , L and X conduction-band minima on the Al content are also shown in the figure. The inset shows the PR spectra of an as-grown $Al_{0.35}Ga_{0.65}As$ sample and a N⁺-implanted $Al_{0.35}Ga_{0.65}N_xAs_{1-x}$ sample. As shown in the figure, the positions of the E_+ and E_- transitions can be well explained assuming an anticrossing



Figure 5. The E_{-} and E_{+} transition energies measured for $Al_yGa_{1-y}N_xAs_{1-x}$ samples. Open circles represent E_0 transitions in samples without N (x = 0). The dependence of the Γ , X and L conduction band edges on the AlAs mole fraction in $Al_yGa_{1-y}As$ alloys are shown by the solid curves. The dashed line represents the estimated change of the E_N position with Al content. The inset shows a comparison of PR spectra measured on the $Al_{0.35}Ga_{0.65}As$ samples with (solid curve) and without (dashed curve) N.

interaction between states at the Γ minimum and a state E_N whose energy depends on the Al content (y) as $E_N = 1.65 + 0.61y$ eV [31]. The results illustrate clearly that an interaction between the X and Γ minima or the L and Γ minima only due to N-induced symmetry breaking, but without taking the N levels into account, as proposed in [23–26], cannot account for the positions of the experimentally observed E_+ and E_- transitions. There is no correlation between the location of the X or L minimum and the E_- and E_+ transition energies. For example, for L- and X-edges located below the Γ edge in Al_yGa_{1-y}As with y > 0.35, it would not be possible for an interaction between Γ and X or between Γ and L to result in the E_+ band edge shifting to an energy position high above the Γ edge.

It has to be pointed out that although the theoretically predicted interactions [23–26] between extended band-edge states do not play any major role in the N-induced modification of the conduction band structure of III–N–V alloys, it is possible that they could be of some significance in those instances where the levels lie close to each other. Such may be the case in GaInNAs at pressures higher than 100 kbar where the X minimum should become resonant with the E_{-} edge. Experimentally, in this case the E_{-} transition shifts to a slightly lower energy with increasing pressures (figure 5). The estimated additional energy shift is of the order of 30 meV. This value is approximately one order of magnitude smaller than the energy shift of the E_{-} edge at atmospheric pressure, resulting from the anticrossing interaction between the Γ edge and the localized N-states.



Figure 6. Comparison of the measured maximum electron concentration with the calculated values as a function of N fraction in $Ga_{1-3x}In_{3x}N_xAs_{1-x}$. Two different cases of the calculated n_{max} are shown: one includes the effects of the downward shift of the conduction band only (dashed curve) and the other includes both the band shift and the enhancement of the density of states (solid curve). The calculated n_{max} for samples without N (i.e. when only the effects from the bandgap lowering produced by In incorporation are considered) are also shown (dotted curve) for comparison. The shaded area indicates the range of Se concentration in these samples.

3.3. Enhancement in maximum free electron concentration

As has been discussed above, the BAC model not only explains the band-gap reduction in dilute III–N–V nitrides but it also predicts that the N-induced modifications of the conduction band will have profound effects on the transport properties of those material systems [27]. In particular, the downward shift of the conduction band edge and the enhancement of the DOS effective mass will lead to much enhanced maximum free electron concentration n_{max} .

The maximum achievable electron and/or hole concentration is of great importance in semiconductor devices engineering. A universal rule that governs the maximum free carrier concentration achievable by doping has been developed based on an amphoteric native defect model and demonstrated to be valid for a wide variety of semiconductor materials [44, 45]. In that model, the type and concentration of the defects compensating intentionally introduced dopants depends on the location of the Fermi level relative to a material-independent common energy reference called the Fermi level stabilization energy $E_{\rm FS}$. GaAs is predicted, for example, to exhibit limitations on the maximum free electron concentration. Indeed, the maximum electron concentration $n_{\rm max}$ in GaAs achievable under equilibrium conditions has been experimentally confirmed to be limited to about $10^{18}-10^{19}$ cm⁻³ [46].

Shown in figure 6 are the free electron concentrations in Se-doped MOCVD-grown $Ga_{1-3x}In_{3x}N_xAs_{1-x}$ films with x = 0-0.033 measured by Hall effect and the electrochemical capacitance–voltage (ECV) technique [47]. Since the Se atomic concentrations in these films are at least an order of magnitude higher than the free electron concentration (in the range of $2-7 \times 10^{20}$ cm⁻³), the measured free electron concentration should be regarded as the maximum

achievable free electron concentration, n_{max} . The result shown in figure 6 indicates that the n_{max} increases strongly with the N concentration. A maximum value of 7×10^{19} cm⁻³ was observed for x = 0.033. This value is ~20 times that found in a GaAs film $(3.5 \times 10^{18} \text{ cm}^{-3})$ grown under the same conditions. The much-enhanced n_{max} in Ga_{1-3x}In_{3x}N_xAs_{1-x} films can be explained by considering the conduction band modifications by a N-induced anticrossing interaction. Since the maximum free electron concentration is determined by the Fermi energy with respect to E_{FS} [46], and because the position of the valence band in GaInNAs is independent of N concentration, the downward shift of the conduction band edge toward E_{FS} and the enhancement of the DOS effective mass in GaInNAs leads to a much larger concentration of uncompensated, electrically active donors for the same location of the Fermi energy relative to E_{FS} . The calculated n_{max} as a function of x for Ga_{1-3x}In_{3x}N_xAs_{1-x} only considering the downward shift of the conduction band anticrossing, as well as that also including the increase in the effective mass, can be obtained using [48].

$$n(E_{\rm F}) = \int \frac{\rho(E) \,\mathrm{d}E}{1 + \exp[(E - E_{\rm F})/k_{\rm B}T]},\tag{6}$$

where $\rho(E)$ is the perturbed density of states. The results are shown in figure 6. Comparison of the experimental data with the calculation shows that in order to account for the large enhancement of the doping limits in III–N–V alloys, both the effects of band-gap reduction and the increase in the effective mass have to be taken into account.

While Se-doped $Ga_{1-3x}In_{3x}N_xAs_{1-x}$ alloys grown by MOCVD have shown enhanced n_{max} in accordance with the BAC model, similar behaviour is also observed in S⁺-implanted GaN_xAs_{1-x} thin films [49]. Figure 7 displays the carrier concentration profiles measured by the ECV technique for S implanted GaN_xAs_{1-x} ($x \sim 0.008$) and SI-GaAs samples after RTA. A striking difference in the free electron concentration n measured in the SI-GaAs and the GaN_xAs_{1-x} samples is observed. In the S⁺-implanted SI-GaAs sample, $n \sim 2.5 \times 10^{17}$ cm⁻³ was measured in the bulk of the implanted layer, with a higher $n \sim 5 \times 10^{17}$ cm⁻³ towards the end of the implantation profile. The theoretical n_{max} in GaN_xAs_{1-x} due to the N-induced conduction band modification within the framework of the BAC model and the amphoteric native defect model is $\sim 1 \times 10^{19}$ cm⁻³ for the $GaN_{0.008}As_{0.992}$ sample. This value is in a reasonably good agreement with the measured concentration of 6×10^{18} cm⁻³ shown in figure 7.

Attempts to form n-type GaN_xAs_{1-x} thin films with high electron concentration were also made by co-implantation of N and a dopant element in GaAs [50]. Figure 8 shows a comparison of the ECV determined free electron concentration profiles for GaAs samples implanted with S alone and co-implanted with S and N (S + N) after RTA at 945 °C for 10 s. The calculated as-implanted S and N atomic distributions are also shown in the figure. The most prominent difference in the electron concentration profiles between the S only and (S + N) samples is the much enhanced electron concentration in the (S + N) sample in a narrow region (~500 Å) near the surface. The region with lower electron concentration at ~0.1–0.2 μ m below the surface coincides with a region with excess As due to the implantation process that makes the substitution of S atoms into the As sites more difficult [50]. In addition, larger concentrations of the compensating V_{Ga} acceptors are also expected in the As-rich region. A reduced availability of group V sites and an increased V_{Ga} concentration in the (S + N) sample where both S and N compete for the same group V element sites.

Considering both band-gap reduction and large increase in the electron effective mass, the high n_{max} in the near-surface region of the (S + N) sample ($\sim 1.5 \times 10^{19} \text{ cm}^{-3}$) implies that the N content in this thin near-surface diluted nitride layer is x = 0.0032. This value is in good



Figure 7. Ionized net donor concentration profiles for the GaN_xAs_{1-x} films and the SI-GaAs standard measured by the electrochemical capacitance–voltage (ECV) technique. The short-dashed curve is the calculated distribution of implanted S atoms. The dashed horizontal lines indicate the theoretical free electron concentrations in $Ga_{1-x}N_xAs$ by considering only the effects of the downward shift of the conduction band (band edge only) and both the effects of band gap reduction and density of states effective mass enhancement (band edge + effective mass).

agreement with the calculated N concentration in the surface region ($x \approx 0.003-0.01$). With this N content the conduction band edge is shifted downward by 77 meV and the conduction band effective mass at the Fermi energy becomes about three times larger than that of GaAs [51].

3.4. Decrease of electron mobility

Incorporation of small amounts of nitrogen into GaAs to form $\text{GaN}_x \text{As}_{1-x}$ leads to a drastic reduction of the electron mobility. The mobility of $\text{GaN}_x \text{As}_{1-x}$ films ranges typically from about ten to a few hundred cm² V⁻¹ s⁻¹ [52, 53]. These values are over an order of magnitude smaller than the electron mobility in GaAs at comparable doping levels. Figure 9 shows the change in room-temperature mobility of $\text{Ga}_{0.93}\text{In}_{0.07}\text{N}_{0.017}\text{As}_{0.983}$:Si with the free electron concentration. The mobility shows a non-monotonic dependence on the electron concentration with a maximum at $n \sim 5 \times 10^{18} \text{ cm}^{-3}$. The room-temperature mobility (μ_1) is calculated from

$$\mu = \frac{e\tau(k_{\rm F})}{m_{-}^{*}(\mathbf{k}_{\rm F})} \approx \frac{e\hbar}{m_{-}^{*}(\mathbf{k}_{\rm F}) \cdot \Gamma_{-}(\mathbf{k}_{\rm F})},\tag{7}$$



Figure 8. The ECV measured net donor concentration profiles for the GaAs samples implanted with S alone and S + N after RTA at 945 °C for 10 s. The calculated atomic profiles for both the implanted S and N are also shown.



Figure 9. Room-temperature electron mobility of $Ga_{0.93} In_{0.07} N_{0.017} As_{0.983}$:Si plotted as a function of electron concentration. The calculated mobilities limited by the conduction band broadening (μ_1) and by the random field scattering (μ_2) are shown. The calculated Fermi energy is referenced to the bottom of the lowest conduction band (E_{-}) .

where $\Gamma_{-}(\mathbf{k}_{\rm F})$ is the broadening of the dispersion relations [48]. The short-dashed curve in figure 9 is the calculated result. Also shown is the Fermi energy as a function of *n* calculated from equation (6). At high electron concentrations, when the Fermi energy approaches the original energy level of the N localized states in In_{0.07}Ga_{0.93}As_{0.983}N_{0.017} (located at ~0.30 eV above the conduction band edge of $E_{\rm M}$, or 0.54 eV above the E_{-} conduction-band edge), the mobility is largely suppressed by the strong hybridization between $|E_{\rm N}\rangle$ and $|E_{\rm M}(k)\rangle$. At $n = 2 \times 10^{19}$ cm⁻³, the energy broadening and the scattering lifetime at the Fermi surface are estimated to be 0.25 eV and 3×10^{-15} s, respectively. The mean free path of free electrons is about 5 Å, which is only a third of the average distance between the randomly distributed N atoms. Therefore, at this electron concentrations the homogeneous broadening resulting from the anticrossing interaction is the dominant scattering mechanism that limits the electron mobility. As is seen in figure 9, at high concentrations the electron mobility calculated from the BAC model is in good quantitative agreement with experiment. It should be noted that this very good agreement has been obtained without any adjustable parameters.

At lower electron concentrations the mobility starts to decrease, deviating severely from μ_1 . This effect can be attributed to the scattering of the conduction electrons by the random fields caused by the structural and compositional disorder in the alloy. It is well known that in partially disordered semiconductors, as the Fermi level decreases from the degenerate doping into the non-degenerate doping regime, the conduction electrons experience increasingly strong scattering from the potential fluctuations. As a result the mobility decreases monotonically with decreasing electron concentration [54, 55]. In the case of GaN_xAs_{1-x} alloys the main contribution to the potential fluctuations originates from the random N distribution. An estimate for the electron mobility limited by the random field scattering (μ_2) is shown in figure 9. The solid curve in the figure includes the contributions from both effects, level broadening and random alloy scattering that limit the overall mobility $\mu = 1/(\mu_1^{-1} + \mu_2^{-1})$. This calculated mobility reproduces the non-monotonic behaviour of the mobility measured over two decades of change in electron concentration.

3.5. Mutual passivation in dilute nitrides

In contrast to the observed enhancement of the doping activation of the group-VI elements (S, Se), co-implantation of Si and N into GaAs was found to only produce highly resistive materials [56]. This asymmetry in the behaviour of groups VI and IV donors reveals an entirely new effect in which an electrically active substitutional group-IV donor and an isovalent N atom passivate each other's electronic effects [57]. This passivation occurs via the formation of nearest neighbour IV_{Ga}–N_{As} pairs in GaN_xAs_{1-x} doped with group-IV donors (Si and Ge).

Figure 10 shows the measured free electron concentration in MBE-grown Si-doped GaAs and Ga_{0.93}In_{0.07}N_{0.017}As_{0.983} epitaxial films, as well as an MOCVD-grown Se-doped Ga_{0.92}In_{0.08}N_{0.024}As_{0.976} thin film after RTA for 10 s in the temperature range 650–950 °C. The Si and Se doping levels in these samples are in the range $2-9 \times 10^{19}$ and $\sim 2 \times 10^{20}$ cm⁻³, respectively. For the GaAs:Si and GaInNAs:Se samples, only slight decreases in electron concentrations, from 1.6×10^{19} to 8×10^{18} cm⁻³ for GaAs:Si and from 3×10^{19} to 2×10^{19} cm⁻³ for GaInNAs:Se, were observed as the result of high temperature RTA. Such a decrease in the electron concentration in GaAs is in agreement with the equilibrium maximum electron concentration (in the range of 10^{18} – 10^{19} cm⁻³) [58]. The much higher electron concentration in the Se-doped GaInNAs sample is also consistent with the enhanced donor activation efficiency resulting from the N-induced modification of the conduction band structure discussed above. On the other hand, however, the free electron concentration in the GaInNAs:Si sample drops from 1.1×10^{19} cm⁻³ in the as-grown film to 3×10^{17} cm⁻³ after RTA at 950 °C for 10 s.



Figure 10. Electron concentrations of Si-doped GaAs and $Ga_{0.93} In_{0.07} N_{0.017} As_{0.983}$ as a function of annealing temperature for 10 s. The dependence of the electron concentration on RTA temperature for a MOCVD-grown Se-doped $Ga_{0.92} In_{0.08} N_{0.024} As_{0.976}$ film is also included.

In fact, RTA at 950 °C for 120 s reduces the electron concentration further down to $<10^{15}$ cm⁻³. The reduced electrical activity of Si donors in GaN_xAs_{1-x} alloys can be attributed to the formation of nearest neighbour Si_{Ga}–N_{As} pairs. The highly electronegative N atom strongly binds the fourth valence electron of Si and effectively deactivates the non-bonding electron. Consequently, the donor activity of the Si is passivated. This picture suggests that, because of the localized nature of the N-states in GaN_xAs_{1-x}, the passivation is limited to group-IV donors that occupy Ga sites. This is supported by the small change in electrical behaviour observed in the GaInNAs:Se thin film in which both the N and Se reside in the As sublattice and therefore cannot form nearest neighbour passivating pairs. It should be pointed out that the mutual passivation effect discussed here differs from the previously observed, much less stable and reversible passivation of the activity of N atoms with hydrogen [59]. In the latter case hydrogen does not have any effect on the material properties by itself.

The well-defined onset temperature of about 700 °C for the observed reduction of electron concentration in GaInNAs:Si shown in figure 10 roughly corresponds to the annealing condition that allows the Si atoms to diffuse over a length equal to the average distance between randomly distributed Si and N atoms (~7 Å) [57]. The diffusion-controlled passivation process is analysed in the context of Si diffusion mediated by both neutral Ga vacancies (V_{Ga}^0) and triply negatively charged Ga vacancies (V_{Ga}^{3-}) [60]. Figure 11 shows the isothermal annealing effects of the normalized free carrier concentration of the GaInNAs:Si sample for annealing temperatures in the range 650–820 °C. Calculations based on Si diffusion via V_{Ga}^0 and V_{Ga}^{3-} vacancies are shown as dashed lines in the figure. The calculations agree very well with the experimental data. According to the diffusion model, at high annealing temperatures or long annealing time, the Fermi-level independent, V_{Ga}^0 -mediated diffusion becomes increasingly important. This is reflected in the fact that the $\ln[n/n_0] \sim t$ curves approach a linear dependence at high temperatures or long anneal times.

Since isoelectronic N is responsible for a massive modification of the electronic structure of GaN_xAs_{1-x} alloys, the question arises to what extent the passivation process affects the N-induced modification of the electronic structure of the alloys. PR measurements on the GaInNAs:Si sample show that the band-gap energy increases with increasing RTA temperature.



Figure 11. Normalized free electron concentration as a function of annealing time at different annealing temperatures. The dashed curves represent the results from analytical calculations based on Si diffusion via Ga vacancies.

Annealing of the sample at 950 °C increases the gap by about 35 meV. If this increase is attributed to deactivation of the N atoms, the concentration of the deactivated N is approximately equal to $0.004 \times 2.2 \times 10^{22}$ cm⁻³ $\approx 8 \times 10^{19}$ cm⁻³, which is close to the initial total Si concentration in the as-grown sample. This is consistent with the formation of Si_{Ga}–N_{As} pairs being responsible for the mutual passivation of both species. This scenario of the passivation process is further corroborated by PL measurements on the GaInNAs:Si sample. A strong PL emission peaked at ~0.8 eV is observed when the sample is mutually passivated, indicating the presence of deep states most likely associated with the Si_{Ga}–N_{As} pairs.

The general nature of the mutual passivation effect is supported by the investigations of GaN_xAs_{1-x} layers doped with Ge, another group IV donor. Ge-doped GaN_xAs_{1-x} layers were synthesized by sequential implantation of Ge and N ions into GaAs followed by a combination of PLM and RTA. The passivation of the N activity by the Ge atoms is illustrated in the series of PR spectra presented in figure 12. The band-gap energies obtained from the PR spectra are shown in the inset as a function of the duration of 950 °C RTA. A fundamental band-gap transition at 1.24 eV is observed for GaAs samples implanted with 2% N alone after PLM-RTA at 950 °C for 10–120 s, corresponding to a GaN_xAs_{1-x} layer with $x \sim 0.01$. In contrast, the band gap of the samples co-implanted with N and Ge (2% N + 2% Ge) after PLM increases from 1.24 to 1.42 eV (band gap of GaAs) as the RTA duration increases to 60 s, revealing that nearly all N_{As} sites are passivated by Ge. The gradual increase in the band gap of the 2% N + 2% Ge sample as a function of RTA temperature and/or time duration can be attributed to the passivation of N_{As} by Ge_{Ga} through the formation of nearest neighbour Ge_{Ga}–N_{As} pairs.

Figure 13 shows a comparison of the electron concentration of the 2% N + 2% Ge and 2% Ge samples followed by PLM-RTA for 10 s in the temperature range 650–950 °C. The electron concentration of both samples approaches 10^{19} cm⁻³ after PLM. For the 2% Ge sample, thermal annealing after PLM drives the system toward equilibrium with an electron concentration of $\sim 1 \times 10^{18}$ cm⁻³ which is consistent with the amphoteric character of Ge in GaAs [61]. The electron concentration of the 2% N + 2% Ge samples, on the other hand, drops over two orders of magnitude to less than 10^{17} cm⁻³ as the samples are subjected to RTA



Figure 12. PR spectra measured from a series of ion beam synthesized Ge-doped $GaN_x As_{1-x}$ samples RTA at 950 °C for durations of 5–120 s. The inset shows the band-gap energies determined from the PR measurements.



Figure 13. Free electron concentrations of the 2% Ge and 2% N + 2% Ge samples after PLM + RTA at increasing temperature for 10 s obtained by Hall effect measurements. Electron concentration for the 2% N + 2% Ge sample after PLM + RTA at 950 °C for 60 s is also shown.

at temperatures higher than 650 °C. The changes in the band gap and the electrical behaviour in the Ge-doped GaN_xAs_{1-x} sample show that the Ge donors and isovalent N passivate each other via the formation of N_{As} -Ge_{Ga} pairs, just as was the case in Si-doped GaN_xAs_{1-x} .

Mutual passivation of Si and N has been also observed in Si-doped $Ga_{0.48}In_{0.52}N_xP_{1-x}$ [62]. All these results clearly demonstrate the general nature of this phenomenon.

4. Conclusions

The effect of N on the electronic band structure in dilute III–N–V nitrides has been explained in terms of a band anticrossing interaction between highly localized N states and the extended conduction-band states of the semiconductor matrix. The interaction leads to a splitting of the conduction band into two non-parabolic subbands. The downward shift of the lower subband edge relative to the valence band is responsible for the reduction of the fundamental bandgap. The profound effects on the optical and electrical properties of the dilute nitrides, such as the significant increase in the electron effective mass and the drastic decrease in the electron mobility, can all be quantitatively accounted for using this model.

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